

# Side-Channel Analysis of Post-Quantum Schemes

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Julius Hermelink – Postdoc

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Max Planck Institute for Security and Privacy

# Who am I?



## Julius Hermelink

### Short CV:

- Postdoc at MPI-SP in Bochum.
- PhD from UniBw in Munich in 2024.
- Master's in Mathematics from LMU in 2020.

### Research interests:

- Implementation attacks on post-quantum schemes.
- Soft-analytic side-channel attacks.
- Cryptanalysis (under side information).
- Information theory.
- How (not) to use formal methods for side-channel security.

# The Quantum Threat

Quantum computers threaten currently used asymmetric cryptography.



We have to assume that:

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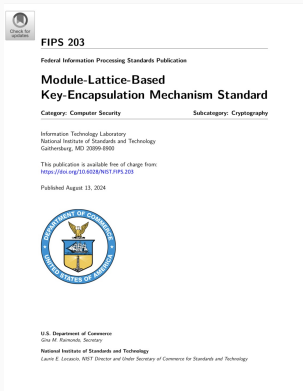
Therefore, we need:

- Post-quantum asymmetric cryptography.
- Most pressing key exchanges.



# The NIST Standardization Process

NIST is in the process of standardizing post-quantum cryptography.

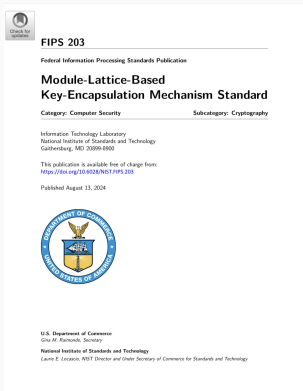


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- Five candidates already selected.
- Three are lattice-based.
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ML-KEM used in Signal, Chrome, iMessage, ...

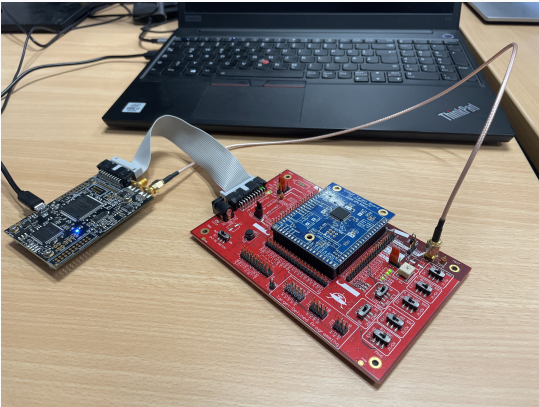


# Side-Channel Attacks

Devices may be vulnerable to side-channel and fault attacks.

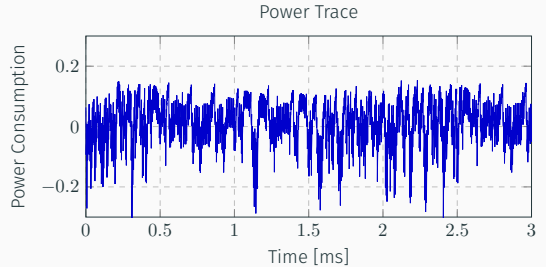
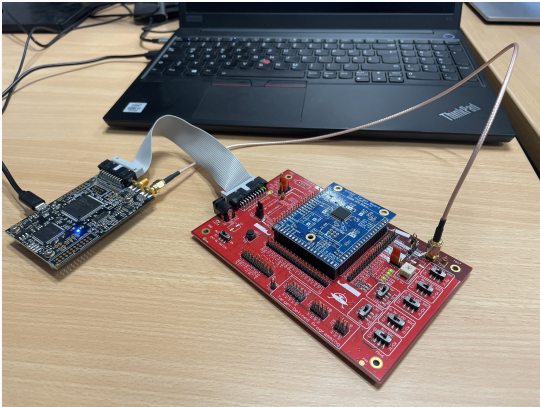
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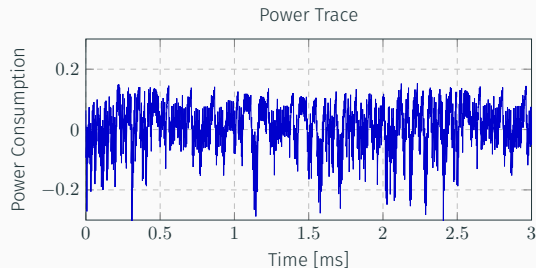
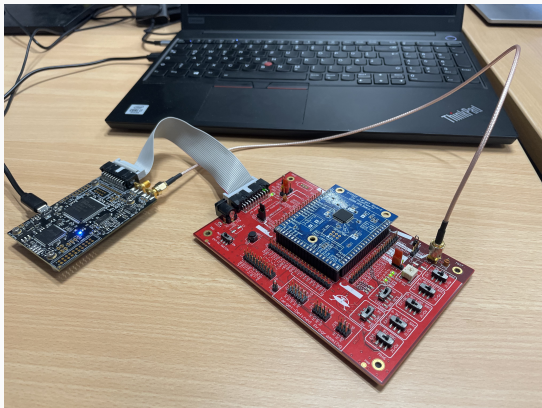
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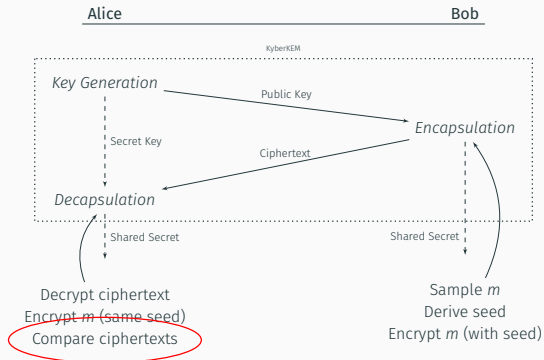
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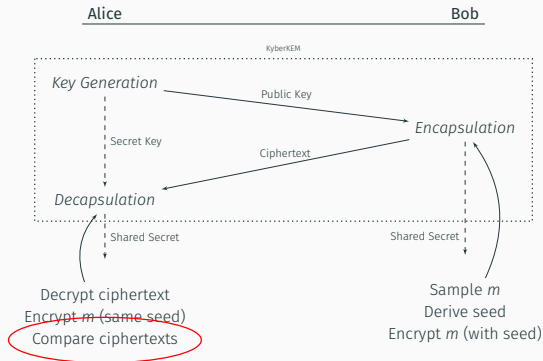


Lattice-based schemes/post-quantum cryptography comes with different challenges.

# New Standards, New Challenges



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In ML-KEM:

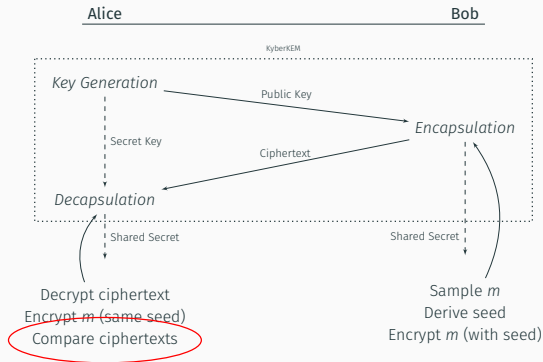
- Comparison  $ct' == ct$ .
- Comparison is sensitive operation.

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$$(-1)^{\text{obs}}(\mathbf{r}^\top \mathbf{e} - \mathbf{s}^\top (\mathbf{e}_1 + \Delta \mathbf{u}) + e_2 + \Delta v) \leq 0$$

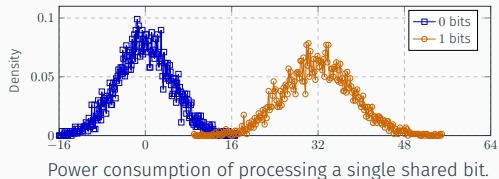
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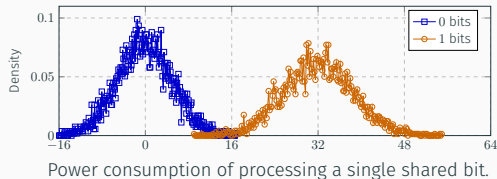
Our model (simulation for  $\sigma = 5$ ):



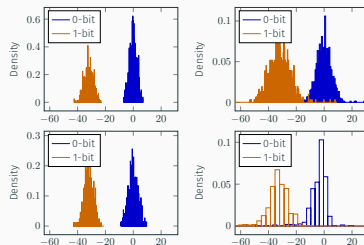
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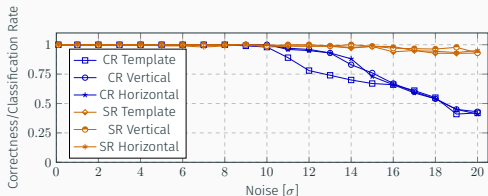
Actual leakage confirms our model:



# Highly Noise-Tolerant Attacks

Leads to highly noise-tolerant attacks.

Simulated results with 4 shares:



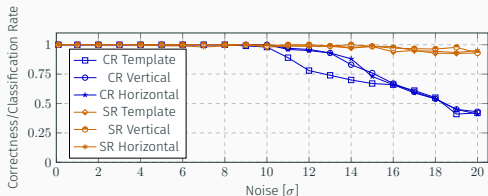
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Why do these attacks work so well?

- Slight advantage enough.
- Amplified leakage.

→ High noise requirements  
– analysis in [HFG+25].

Noise/masking order necessary to prevent attacks extraordinarily high.

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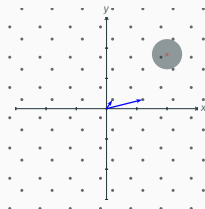
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# Side Information in Lattice-Based Schemes

How to deal with side information in lattice-based schemes?

Primal attack:

E.g., [DDGR20; DGHK23; MN23]

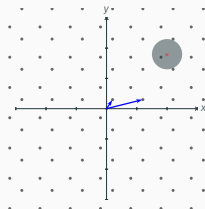


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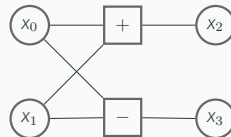
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Soft-analytic [VGS14]:

E.g., [PPM17; tPP21; BAE+24]



Attacks: often noisy information on Hamming weights.



Various proposals to define and deal with side information.

Previous hint definitions [DDGR20; DGHK23]:

For known  $\mathbf{v}, l, k$ :

- $\langle \mathbf{v}, \mathbf{x} \rangle = l$
- $\langle \mathbf{v}, \mathbf{x} \rangle = l \bmod k$
- $\langle \mathbf{v}, \mathbf{x} \rangle = l + \mathcal{N}$
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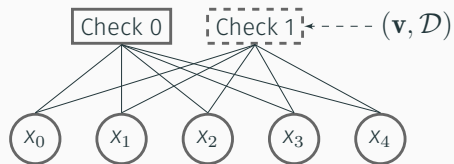
Information from [RPJ+24] without loss!

$$\text{HW}(\langle \mathbf{v}, \mathbf{x} \rangle) \sim \mathcal{D}$$

Two different solvers: BP and Greedy

# Solving Distribution Hints

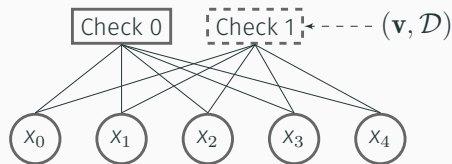
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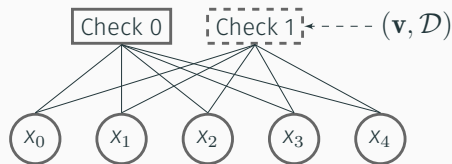
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$$P(x_j = x'_j) = \sum_{a \in \text{supp } \mathcal{D}} P_{\mathcal{D}}(a) P\left(\sum_{i \neq j} v_i x_i = a - v_j x'_j\right)$$

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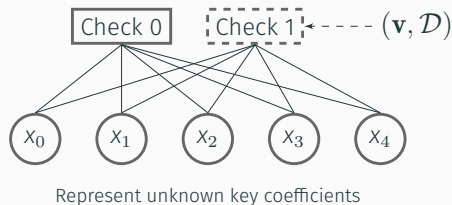
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Greedy:  $\mathbf{x}'$  and change  $x_j + c$ .

Change scores for coefficients  $j$ :

$$s_j(c) = \sum_{a \in \text{supp } \mathcal{D}} P_{\mathcal{D}}(a) |\langle \mathbf{v}, \mathbf{x}' \rangle + v_j c - a|,$$

and perform  $k$  best updates on guess  $\mathbf{x}'$ .

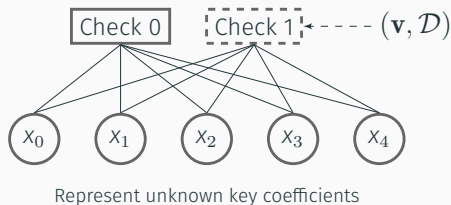
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$$P\left(\sum_{i \neq j} v_i x_i = a - v_j x'_j\right) \rightarrow |\mathbf{v}^T \mathbf{x}' + v_j c - a|$$

# Side-Channel Attacks on Masked ML-DSA

A more conceptual approach to side-channel attacks on ML-DSA.

Masked ML-DSA:

- Different types of masking.
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- Several attacks on unmasked ML-DSA.

How to target masked ML-DSA?

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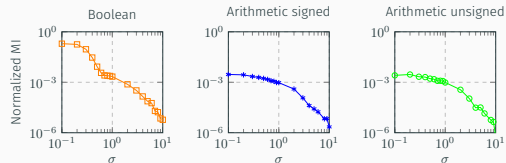
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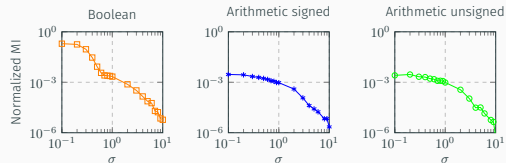
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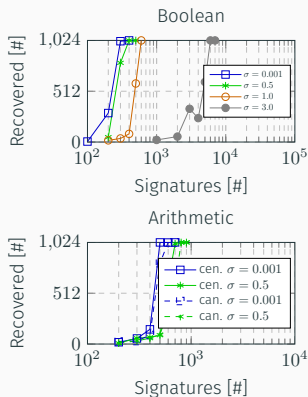


Our framework can be applied with hint-filtering technique.

First attacks against masked ML-DSA targeting  $y$  in several representations.

Practical attacks:

- Replicates previous attack.
- New reasonably noise-tolerant second-order attacks.
- Concrete practical recommendations for future implementation.



# Conclusion

## Conclusion:

- Protecting ML-KEM is challenging.
- Efficient and generic framework.
- Attacks on masked ML-DSA.
- Works well with info-theoretic analysis.
- Framework applies more generally.

## Open source:



## Easy to use!

```
bp = PyBP(vs, distributions)
greedy = PyGreedy(vs, distributions)
greedy.set_nthreads(4)
bp.set_nthreads(4)

greedy.solve(k)
guess = greedy.get_guess()
bp.propagate()
dists = bp.get_results()
```

Thank you for your attention!

# References (1)

- [BAE+24] Olivier Bronchain, Melissa Azouaoui, Mohamed ELGhamrawy, Joost Renes, and Tobias Schneider. “Exploiting Small-Norm Polynomial Multiplication with Physical Attacks Application to CRYSTALS-Dilithium”. In: *IACR Transactions on Cryptographic Hardware and Embedded Systems 2024.2* (2024), pp. 359–383.
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